

(5) Suppose you are trying to prove  $\lim (3x - 7) = -4$  Given  $\varepsilon > 0$  what value must  $\delta$  be in order to satisfy  $x \rightarrow 1$ 

(No need to show formal proof) the definition of limit?

(4 points)

(6) (a) Give the <u>formal/rigorous</u> definition for  $\lim_{x \to a^+} f(x) = L$ 

(9 points)

(b) Give the <u>formal/rigorous</u> definition for  $\lim_{x \to a} f(x) = -\infty$ 

(c) Give the formal/rigorous definition for 
$$\lim_{x \to \infty} f(x) = \infty$$



(8) Evaluate the following limits if they exist (if the limit is ∞ or -∞ say so.). No proof or detailed steps necessary, but do show work. ( 4 points each )

(a) 
$$\lim_{x \to -2} \sqrt[3]{5+x^5} =$$
 (b)  $\lim_{x \to 3} \frac{x-3}{x^2-9} =$ 

(c) 
$$\lim_{x \to 16} \frac{16-x}{\sqrt{x-4}} =$$
 (d)  $\lim_{x \to 4^-} \frac{x-5}{x(x-4)} =$ 

(9) Prove that there is at least one solution to the equation cosx = x (4 points)
 *Hint: If you are going to use a theorem, name the theorem and verify any hypotheses are satisfied.*

(10) For what values of x are the following functions continuous? Show work. (4 points each)

a) 
$$f(x) = \frac{2x+3}{\sin x - 1}$$
  
b)  $f(x) = \sqrt{x^2 - x - 6}$   
c)  $f(x) = \begin{cases} 5x+2 & \text{if } x > 0\\ \sqrt{4-x} & \text{if } x \le 0 \end{cases}$ 

- (11)The displacement (in meters) of an object moving in a straight line is given by  $s = t^2 3t$ , where t is measured in seconds.
  - (a) find the average velocity over the time period [4,5]
  - (b) using methods discussed in this class, find the instantaneous velocity when t=4. (7 pts)

(2 pts.)

Answer should have the appropriate units.

(12) Using methods discussed in class,

- a) Use an appropriate form of the definition of the derivative to compute f'(a) if  $f(x) = \frac{1}{x}$ .
  - (6 pts)
- b) Use the results of part (a) to find the slope of the tangent line at x = -1, 1/2, and 3. (3 pts)
- c) Sketch a graph of f(x) and the tangent line at x=3. Based on your graph, Is your answer in part
  (b) reasonable? Explain (4 pts)
- d) Find the equation of the tangent line at x=3.

(3 pts)

